Great Appreciations: Accounting for the Real Exchange Rate in Mexico, 1988-2002

Felipe Meza
Instituto Tecnológico Autónomo de México
and
Carlos Urrutia
Instituto Tecnológico Autónomo de México
and
Georgetown University

October 2008
Discussion Paper 08-07
Great Appreciations:

Accounting for the Real Exchange Rate in Mexico, 1988-2002

Felipe Meza
Centro de Investigación Económica, ITAM

Carlos Urrutia
Centro de Investigación Económica, ITAM

Georgetown University

This version: March 2009

Abstract

Between 1988 and 2002 the real exchange rate in Mexico appreciated by 40%, of which more than three-fourths is explained by a decline in the domestic relative price of tradable goods. We account for this decline using a two sector dynamic general equilibrium model of a small open economy, with non-tradable goods and frictions to labor reallocation. The model allows us to identify the effect of the differential in productivity growth across sectors (the Balassa-Samuelson effect) from other types of shocks affecting the allocation of resources. We find that productivity growth in the tradable sector and a decline in the real interest rate faced by Mexico in the international markets account for about 60% of the decline in the domestic relative price of tradables. Our model is also consistent with the observed reallocation of labor from tradable to non-tradable sectors. The results are robust to the inclusion of terms of trade into the model. We do not find a significant role for migration remittances, foreign reserves accumulation, government spending, or import tariffs.

‡This paper has benefited from comments by Enrique Mendoza, Behzad Diba, Rudolf Bems, Daniel Chiquiar and participants in seminars at the International Monetary Fund and Banco de Mexico. We would like to thank especially Sangeeta Pratap for giving us access to her databases. The support of CONACYT through research grant No. 81825 is thankfully acknowledged. All errors are our own. Contact Information: felipe.meza@itam.mx, ceu3@georgetown.edu.
1 Introduction

Between 1988 and 2002 Mexico experienced a substantial appreciation of its real exchange rate (RER). In spite of the 1995 crisis, in which the RER briefly depreciated as a result of a sudden stop of loans from abroad, the trend in the whole period shows a 40% appreciation. Similar episodes of RER appreciation have been observed in other Latin American countries (for example, Argentina 1991-2001, Brazil 2002-07, and Chile 1986-98). In all these cases, including Mexico, the appreciation coincides with a period of financial liberalization, capital inflows and trade deficits.

In this paper we switch the focus of our analysis from the short run effects of the 1995 crisis to the long run trend observed in Mexico between 1988 and 2002. We use a structural model to analyze the relation between the RER appreciation and different supply and demand shocks affecting the Mexican economy. Building a model allows us to establish causality and decompose the underlying transmission mechanisms. Making this model quantitative, through a careful calibration of the main parameters, allows us to measure its success in generating an appreciation similar to the one observed in the data.

Looking at the Mexican data for the period, we document the following stylized facts: (i) 78% of the RER appreciation corresponds to a decline in the domestic relative price of tradable goods, measured as the GDP deflator in the tradable goods sectors divided by the overall GDP deflator; (ii) changes in relative outputs and relative wages across sectors are an important component of the story, but changes in factor income shares are not; (iii) growth accounting for each sector reveals an increase in measured TFP in the tradable sector, while TFP remains stagnant in the non-tradable sector; and (iv) there is a substantial reallocation of resources (capital and labor) from the tradable sector towards the non-tradable sector during this period.

These regularities, in particular fact (iii), seem consistent with an explanation of the Mexican appreciation based on the Balassa-Samuelson hypothesis: technological progress in the tradable sector reduces the cost of production, making tradable goods cheaper and reducing their relative value with respect to non-tradable goods. One of our objectives is to provide a quantitative assessment of this mechanism in explaining the decline of the domestic
relative price of tradable goods in Mexico. For this, our model also needs to be consistent with stylized facts (ii) and (iv), in particular with the reallocation of labor over time from the tradable to the non-tradable sector.

Differential TFP growth is only half of our story. Financial liberalization and the opening of the capital account increased the ability of the Mexican economy to borrow in international markets. The interest rate for loans to Mexico, including the country risk premium, fell from around 20% in the late eighties to less than 5% in 2002, with a short run jump during the 1995 crisis. As the ability to borrow increases, so does the trade deficit and the relative value of non-tradable goods, which cannot be imported. This mechanism is then also potentially able to produce a RER appreciation as the one observed in Mexico.

We build a two sector, deterministic, dynamic general equilibrium model of a small open economy that can accommodate both supply shocks (such as sectoral TFP changes) and demand shocks (such as the reduction in the international interest rate). The model is real, abstracting from a monetary side, and constrained-efficient, in the sense that in spite of adjustment costs to capital accumulation and labor mobility the competitive equilibrium is Pareto-optimal. This distinguishes our analysis from alternative stories based on price rigidities, imperfect competition, and so on.

We calibrate the model to some aggregate statistics for the Mexican economy. In particular, we use an input-output matrix to calibrate the technology parameters for each sector. Starting from a stationary equilibrium, we feed the model with the exogenous paths for TFP in each sector and the international interest rate for Mexico, and obtain time series for relative prices and other variables of interest generated by the model. Our model accounts for 60% of the change in the domestic relative price of tradable goods observed in the data. The model is also consistent with the evolution of relative wages and the size of the reallocation of labor towards the non-tradable sector. The results are robust to the introduction of international goods differentiation and terms of trade shocks. Moreover, adding other demand shocks to the model, such as migration remittances, changes in foreign reserves and government expenditures, and import tariffs reduction following NAFTA, does not change our results nor do these shocks contribute significantly to account for the Mexican appreciation.
Our exercise closely relates to the literature of "Great Depressions", summarized in Kehoe and Prescott (2007) with an early application to the Mexican economy in Bergoeing et al. (2002). As in the basic approach, we identify shocks in the data (including, but not limited to, TFP shocks) which are then fed into a calibrated neoclassical growth model (extended, in our case, to a two sector open economy framework). Also following this literature, ours is basically an accounting exercise: we assess quantitatively the impact of these shocks on our variable of interest (the domestic relative price of tradable goods, as opposed to GDP per worker in the "Great Depressions" literature) while checking the consistency of other predictions of the model (such as the reallocation of labor across sectors) with the data.

Calibrated open economy growth models have been successfully used to understand the 1995 crisis in Mexico and its effect on real GDP. A few recent examples include Kehoe and Ruhl (2009), Meza (2008) and Pratap and Urrutia (2008). Some of these exercises have implications for the evolution of the RER during the sudden stop. In particular, Kehoe and Ruhl (2009) do obtain an RER appreciation after a jump at the beginning of the crisis. However, in their model this is driven mostly by changes in terms of trade, rather than changes in the domestic relative price of traded goods. Our empirical analysis shows that for the whole 1988-02 period the latter are more important. Their model also abstracts from sector-specific TFP shocks, although it does include changes in the international interest rate.

Our analysis also borrows from the structural transformation literature, which focuses on the long run reallocation of labor across sectors. Ngai and Pissarides (2007) study how differences in TFP growth rates across sectors lead to structural change in a model with an investment and a consumption sector, while Guerrieri and Acemoglu (2008) study how differences in capital shares across sectors lead to more rapid growth of employment in less capital-intensive sectors. In the context of our model, the tradable sector includes manufacturing, which is an investment good produced in a capital intensive industry, while the non-tradable sector can be mapped into the consumption, labor intensive sector. Differently to these papers, we analyze the process of structural transformation in an open economy model and show that the ability to borrow from abroad is key to understand the size and the speed of labor reallocation across sectors.
Finally, our paper also relates to the empirical literature on the Balassa-Samuelson effect and the long run determinants of the RER (see, for example, Asea and Mendoza (1994), Canzoneri, Cumby and Diba (1999), and Choudhri and Khan (2005)). The results offer mixed support for the Balassa-Samuelson hypothesis. Our approach is different, though, in that we use a structural model to evaluate the impact of sectoral TFP shocks measured from the data.

The paper is organized as follows. In Section 2 we discuss the evidence from the 1988-02 Mexican data. Section 3 introduces the model, while the calibration and the main quantitative exercise is described in Section 4. In Section 5, we discuss in more detail the mechanisms driving our results and perform some sensitivity analysis with respect to other demand shocks. Section 6 modifies the basic model to allow for international good differentiation and terms of trade shocks. Finally, we conclude.

2 Looking at Mexican Data: 1988-2002

The first step in our investigation is to look carefully at the RER appreciation in Mexico between 1998 and 2002. We show that a fall in the domestic relative price of tradable goods accounts for about 78% of the real appreciation. We also provide a decomposition of the changes in the relative price of tradable over non-tradable goods which guides our choice of a model in the next section. Finally, we perform sectoral growth accounting exercises for the tradable and non-tradable sectors and identify TFP shocks (Solow residuals) affecting their relative productivity.

2.1 Real Exchange Rate and Relative Prices

We construct the bilateral, GDP based real exchange rate for Mexico against the US using the standard definition:

\[ RER \equiv \frac{eP^*}{P} \]

where \( e \) is the nominal exchange rate (pesos per dollar) and \( P \) and \( P^* \) are the GDP deflators in Mexico and the US. Figure 1 displays the time series for this variable between 1998 and
2002, normalized to take the value 100 in 1988 (as most series in the following graphs). Our measure shows a large 40% appreciation in the RER for Mexico between 1988 and 2002 together with a sharp, but short lived, depreciation during the 1995 crisis. We focus in this paper on the long run negative trend, instead of the short run spike of 1995.

Figure 1 also compares our measure of the RER against a multilateral, CPI based measure reported by the Mexican central bank, Banco de Mexico. This is relevant since there are relative advantages and disadvantages of using CPI or GDP deflators as price indices in the RER. Also, it helps us to check if using the US to represent the whole scope of Mexican foreign exchange is a good approximation. Figure 1 shows that these two measures are very similar and capture the same long run trend. If anything, the multilateral CPI based RER features more volatility, with a larger depreciation during the 1995 crisis and a bigger appreciation (45% instead of 40%) over the whole period. We choose to continue the analysis with our bilateral GDP based RER since it is easy to map into the NIPA system, allowing for some of the decompositions that follow.

2.1.1 Real Exchange Rate and the Domestic Relative Price of Tradables

Measuring prices consistently, the following identity holds:

\[ RER \equiv \frac{eP^*}{P} = \left( \frac{eP^*}{P^T} \right) \left( \frac{P^T}{P} \right) \]  

The second term \( P^T/P \) is the price of domestic tradable goods relative to the domestic aggregate price level (we will refer to this price in short as the *domestic relative price of tradables*). The first term \( eP^*/P^T \) is a *residual* which captures deviations from the price of Mexican tradable goods with respect to the foreign price level.

The decomposition is useful because standard neoclassical models of the small open economy are silent about this residual. If anything, a two-sector version with non-tradable goods can generate deviations between the domestic prices of tradable goods and the aggregate price level. With a weight \( \gamma \) of tradable goods in the aggregate price level, we can
approximate the domestic relative price of tradables by:

\[
\frac{P^T}{P} \approx \left( \frac{P^T}{P^N} \right)^{1-\gamma}
\]  \hspace{1cm} (2)

Hence changes in the relative price of the tradable good over the non-tradable good \( P^T/P^N \) could provide a potential explanation of movements in the domestic price of tradables and the RER. However, if the economy is small and markets are competitive, the relation between the price of tradables in the domestic market and the foreign price level is exogenous, so the model has no explanatory power with respect to it.

It is then relevant to assess the quantitative importance of the two channels in explaining the RER appreciation in Mexico. We construct a time series for the domestic relative price of tradables in Mexico dividing the sectoral value added for tradable sectors by the GDP deflator, both obtained from NIPA.\(^1\) Figure 2 compares this price to the GDP based bilateral RER. As shown, the decline in the domestic relative price of tradables is the key component to understand the RER appreciation in Mexico. In a crude decomposition, looking only at endpoints, the decline in the domestic relative price of tradables accounts for 78% of the change in the RER. Changes in the residual as defined in equation (1) are much smaller in the long run, although they seem to explain the 1995 jump.

Based on this observation, we use a competitive model of a small open economy to account for the change in the domestic relative price of tradables (via the relative price of tradable over non-tradable goods) as our first approximation to understand the long run RER appreciation in Mexico.

2.1.2 Terms of Trade and the Residual

The residual in equation (1) could be capturing different things: Terms of trade, transportation costs, price of non-tradables abroad, foreign exporters’ mark-ups, and so on. Perhaps surprisingly, Figure 3 shows that most of the long run behavior of the residual for Mexico is

\(^1\)In our data analysis we follow the convention of including manufacturing, agriculture, mining and fishing activities as part of the traded good sector. All other activities (in particular, services, construction) are treated as part of the non-traded sector. Deflators for each sector are computed dividing value added at current prices by value added at constant (1993) prices.
captured by the inverse of the terms of trade (i.e., the relative price of imports over exports, computed again using deflators from NIPA). The correlation between these time series is also high (0.79), although the residual shows more volatility in particular during the 1995 crisis.

Product differentiation by country of origin can provide an explanation for differences in the prices of exports and imports even in the context of competitive, small open economy models. We will add this feature to a second version of our model to see how robust our results on the domestic relative price of tradables are to exogenous changes in the residual, driven by terms of trade shocks.

2.1.3 An Alternative Decomposition of the RER

Following Engel (1999), we can also decompose the RER in the following two components:

\[
RER \equiv \frac{eP^*}{P} = \left( \frac{eP^T*}{P^T} \right) \left( \frac{P^T}{P^T*} \right)
\]

The second term is the domestic relative price of tradables divided by the foreign relative price of tradables. The first term captures deviations in the law of one price in tradable goods. Engel (1999) provides a variance decomposition of the RER for the US and shows that deviations in the law of one price in tradable goods are more important than previously thought. Mendoza (2005) confirms this result for Mexico. Using a time frame comparable to ours, Kehoe and Ruhl (2009) calculate that deviations in the law of one price in tradable goods account for about 65% of the changes in the RER in Mexico.

This result does not contradict our conclusion that most of the action in explaining long run RER movements in Mexico lies in the domestic relative price of tradable goods. Indeed, this price fell in Mexico by 33% between 1988 and 2002, a big change with important effects on the allocation of resources inside the Mexican economy. By construction, Engel-style decompositions underestimate the role of the domestic relative price of tradable goods if similar changes in prices are also observed in foreign countries. But for the purpose of our paper, changes in the foreign relative price of tradable goods are irrelevant, as they are
Table 1: Decomposition of the Relative Price of Tradable over Non-Tradable Goods

<table>
<thead>
<tr>
<th>Contribution (%)</th>
<th>Relative Price (T/N)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(1) Relative Wages (T/N)</td>
<td>24%</td>
</tr>
<tr>
<td>(2) Relative Labor Income Shares (N/T)</td>
<td>10%</td>
</tr>
<tr>
<td>(3) Relative Output per Worker (N/T)</td>
<td>66%</td>
</tr>
<tr>
<td>(1)+(3)</td>
<td>90%</td>
</tr>
<tr>
<td>(1)+(2)+(3)</td>
<td>100%</td>
</tr>
</tbody>
</table>

Table 1: Decomposition of the Relative Price of Tradable over Non-Tradable Goods

exogenous for a small open economy and, contrarily to terms of trade shocks captured by our residual defined in (1), they do not affect domestic decisions.

2.2 More on the Relative Price of Tradable over Non-Tradable Goods

We present a decomposition of the relative price of tradable over non-tradable goods that will guide our modelling choices in the next section. According to (2), the domestic relative price of tradable goods can be approximated by a concave function of the relative price of tradable over non-tradable goods. The following identity provides a useful decomposition:

\[
\frac{P_T}{P_N} = \left( \frac{W_T}{W_N} \right) \left( \frac{W_N L_N / P_N Y_N}{W_T L_T / P_T Y_T} \right) \left( \frac{Y_N / L_N}{Y_T / L_T} \right)
\]

Relative Wages  Relative Labor Income Shares  Relative Output per Worker

Note that this formula is indeed an identity and will hold for any economy as long as the data that we feed into it is collected in a consistent way.

Changes in the relative price of tradable over non-tradable goods can be accounted for by: (i) movements in the relative average wage, (ii) changes in the relative labor income shares, and (iii) movements in the relative output per worker. Using Mexican data, Figure 4 plots each of the three components against the relative price.\(^2\) Table 1 summarizes the results of the decomposition, looking only at endpoints.

Notice first that, even though relative labor income shares are far from constant over

\(^2\)In these series, output for each sector corresponds to sectoral GDP (value added) at constant prices, the number of workers are obtained from employment series by sector, and nominal wages for each sector are computed as the ratio of the wage bill (at current prices) divided by the number of workers.
time, they do not display any significative long run trend. Not surprisingly, their overall impact on relative prices is small. We use this evidence to justify our choice of a Cobb-Douglas production function in the model that follows, instead of a setup in which labor income shares vary over time. By this choice we lose some action, but our decomposition shows that we miss less than 10% of the change in the variable that we want to explain, in exchange for tractability.

According to our decomposition, everything else equal relative prices and relative wages should be directly related. In the Mexican data, they are. Between 1989 and 1996, wages grew at a faster rate in the non-tradable sector, although from 1997 onwards relative wages are largely flat. Overall, changes in relative wages account for 24% of the fall in the relative price of tradable over non-tradable goods. This evidence suggests that deviations from wage equalization across sectors play a role in explaining the RER appreciation. Our model will feature a labor market friction which will be consistent with this property of the data.

In contrast, the observed decline in relative output per worker of the non-tradable sector against the tradable sector is indeed large and accounts for 66% of the fall in the relative price of tradable over non-tradable goods. Adding the contribution of output per worker and relative wages we account for 90% of the decline in this relative price. For this, it is key that over the 15-year period analyzed in the data output grew consistently at a faster rate in the tradable sector. We now analyze more deeply what is behind these productivity changes using growth accounting.

### 2.3 Sectoral Growth Accounting

Inspired by the previous discussion, we continue our analysis by imposing a Cobb-Douglas production function in each sector:

\[
Y_t^i = A_t^i \left( K_t^i \right)^{\alpha_i} \left( L_t^i \right)^{1-\alpha_i}
\]

for \( i = T, N \). From this equation, we compute the implied total factor productivity (TFP) factors as

\[
\hat{A}_t^i = \frac{Y_t^i}{ \left( K_t^i \right)^{\alpha_i} \left( L_t^i \right)^{1-\alpha_i} }
\]
Table 2: Sectoral Growth Accounting

<table>
<thead>
<tr>
<th>Annualized Growth Rate (%)</th>
<th>Output</th>
<th>Capital</th>
<th>Labor</th>
<th>Implied A</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Tradable Sector</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>1988-93</td>
<td>3.5%</td>
<td>2.7%</td>
<td>0.2%</td>
</tr>
<tr>
<td></td>
<td>1993-98</td>
<td>4.4%</td>
<td>4.7%</td>
<td>1.1%</td>
</tr>
<tr>
<td></td>
<td>1998-02</td>
<td>1.5%</td>
<td>-0.1%</td>
<td>-0.5%</td>
</tr>
<tr>
<td></td>
<td>1988-2002</td>
<td>3.3%</td>
<td>2.6%</td>
<td>0.3%</td>
</tr>
<tr>
<td></td>
<td>Non-tradable Sector</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>1988-93</td>
<td>4.0%</td>
<td>6.2%</td>
<td>4.0%</td>
</tr>
<tr>
<td></td>
<td>1993-98</td>
<td>2.4%</td>
<td>2.3%</td>
<td>2.8%</td>
</tr>
<tr>
<td></td>
<td>1998-02</td>
<td>3.3%</td>
<td>6.5%</td>
<td>1.3%</td>
</tr>
<tr>
<td></td>
<td>1988-2002</td>
<td>3.2%</td>
<td>5.1%</td>
<td>2.8%</td>
</tr>
</tbody>
</table>

using data for sectoral output (VA at constant prices), labor (employment) and capital (also at constant prices). Data for capital stocks is obtained from Banco de Mexico surveys, and is consistent at the sectoral level with the perpetual inventory method. We use the factor shares $\alpha^T = 0.48$ and $\alpha^N = 0.35$, whose values will be discussed in detail in the calibration section.

Table 2 and Figure 5 report the implied TFP factors obtained from the formula above. TFP in the tradable sector grew on average at a 2.2% annual rate relative to TFP in the non-tradable sector. This rate does not change significantly over time, and it is mostly driven by the growth in $A_T$. At the same time capital and labor reallocate from the tradable sector towards the non-tradable sector, as shown in Figure 6.

This evidence characterizes a period of structural transformation of the Mexican economy which is consistent with an explanation of the RER appreciation based on the Balassa-Samuelson hypothesis, this is, based on the differential productivity growth between tradable and non-tradable sectors. We explore how far we can we go with this hypothesis in the next section, when we feed a dynamic two-sector general equilibrium model of the economy with the measured sectoral TFPs. A successful model should deliver not only the right change in relative prices between the two sectors, but also the observed factor reallocation.
3 A Two-Sector Model of a Small Open Economy

We build a simple two sector dynamic general equilibrium model of a small open economy. This model provides a natural laboratory to analyze the impact of sectoral TFP and demand shocks on the relative price of tradable and non-tradable goods and on the allocation of capital and labor across sectors.

3.1 Production

The economy produces two intermediate goods, one of which is tradable while the other cannot be traded with the rest of the world. Each intermediate good is produced combining capital and labor through a Cobb-Douglas technology:

\[ Y_i^t = A_i^t (K_i^t)^{\alpha_i} (L_i^t)^{1-\alpha_i} \quad i = T, N. \]

Capital and labor are rented from consumers. A final good is produced using tradable and non-tradable goods as inputs, using the CES aggregator

\[ Y_t = \left[ \gamma (Q_T^t)^\rho + (1 - \gamma) (Q_N^t)^\rho \right]^{\frac{1}{\rho}} \]

where \( Y_t \) is the output of the final good (it will also be equal to domestic absorption in our model), \( Q_T^t \) and \( Q_N^t \) are quantities of each intermediate good and \( \rho \) determines the elasticity of substitution, which is \( 1/(1 - \rho) \).

There is one representative firm in each sector which takes prices as given. The profit-maximization problem for the intermediate producer of good \( i = T, N \) is

\[
\max_{Y_t^i, L_t^i, K_t^i} \left\{ p_T^i Y_t^i - w_T^i L_t^i - r_t K_t^i \right\}
\]

s.to \( Y_t^i = A_t^i (K_t^i)^{\alpha_i} (L_t^i)^{1-\alpha_i} \)

for all \( t \), where the price of tradable and non-tradable goods (\( p_T^t \) and \( p_N^t \)), the sector specific wage rates (\( w_T^t \) and \( w_N^t \)) and the common rental rate of capital \( r_t \) are all expressed in units
of the final good. As we will see, capital is freely mobile across sectors, but there are frictions to labor reallocation that prevent wages to equate across sectors.

Similarly, the producer of the final good solves each period the static problem:

$$\max_{Y^T_t, Q^T_t, Q^N_t} \{Y_t - p^T_t Q^T_t - p^N_t Q^N_t \}$$

s.t. $$Y_t = \left[ \gamma \left( Q^T_t \right)^{\rho} + (1 - \gamma) \left( Q^N_t \right)^{\rho} \right]^{\frac{1}{\rho}}$$

Note that the final good producer does not add any value added to the economy. GDP at current prices will be given by the sum of value added by the tradable and non-tradable intermediate good sectors:

$$GDP_t = p^T_t Y^T_t + p^N_t Y^N_t$$

while real GDP (at constant prices) is constructed using some base year prices:

$$RGDP_t = p^T_0 Y^T_t + p^N_0 Y^N_t$$

### 3.2 Consumption and Savings

A representative consumer is endowed with $K_0$ units of initial capital, $B_0$ units of foreign bonds, and a sequence $\{L_t\}_{t=0}^{\infty}$ of labor endowments supplied inelastically to the market. Consumers’ intertemporal preferences are summarized by the CRRA lifetime utility function:

$$\sum_{t=0}^{\infty} \beta^t \left[ \frac{(C_t/L_t)^{1-\sigma} - 1}{1-\sigma} \right]$$

where $C_t$ represents consumption of the final good and $\beta \in (0, 1)$ is the discount factor. Income is obtained from renting labor to each sector, at wage rates in units of the final good $w^T_t$ and $w^N_t$, and renting capital at a common rental rate $r_t$. The representative consumer decides how much to consume, how much to invest in new capital and new foreign bonds, and the fraction of his/her labor endowment $\theta_t$ supplied to the tradable sector.
The budget constraint for each period is:

\[ C_t + K_{t+1} + p_T^t B_{t+1} = w_t^T \theta_t L_t + w_t^N (1 - \theta_t) L_t + [r_t + (1 - \delta)] K_t \]

\[ + (1 + r_T^*) p_T^t B_t - \frac{\psi}{2} \left( K_{t+1} - K_t \right)^2 - \frac{\phi}{2} (\theta_t - \theta_{t-1})^2 \]

where \( \{r_T^*\}_{t=0}^{\infty} \) is an exogenous sequence of world interest rates, \( \delta \in (0, 1) \) is the depreciation rate and the parameters \( \psi, \phi > 0 \) indicate the magnitude of the quadratic adjustment costs to change the stock of capital and to move labor across sectors. Our intuition for the latter is that changing sectors implies for workers some loss of sector-specific human capital, whose cost is paid by the representative consumer according to this ad-hoc function. The initial allocation of labor across sectors inherited from the past \( (\theta_{-1}) \) is exogenously given.

The representative consumer maximizes lifetime utility subject to the budget constraint above. Notice that consumption and investment imply purchases of the same final good (or, alternatively, tradable and non-tradable goods are combined in the same way to produce consumption and investment goods). We choose this specification for simplicity, even though it abstracts from changes in the relative price of investment over consumption goods. Note also that the foreign bond and its exogenous return are also denominated in (real) units of the tradable good.

### 3.3 Equilibrium

The model is closed by imposing the following market clearing conditions: (i) for the final good

\[ C_t + K_{t+1} - (1 - \delta) K_t + \frac{\psi}{2} \left( \frac{K_{t+1} - K_t}{K_t} \right)^2 + \frac{\phi}{2} (\theta_t - \theta_{t-1})^2 = Y_t \]

(ii) for each intermediate good

\[ Q_T^t + N X_T^t = Y_T^t \quad Q_N^t = Y_N^t \]

where \( N X_T^t \) represents net exports of the tradable good, and
(iii) for production factors

\[ K_t^T + K_t^N = K_t \quad \theta_t L_t = L_t^T \quad L_t^N = (1 - \theta_t) L_t \]

In this setup, the current account can be constructed as the value of net exports plus interest payments or as the change in the foreign asset position:

\[ CA_t \equiv NX_t^T + r_t^* B_t = B_{t+1} - B_t \]

Notice that GDP (at current prices) can be constructed according to NIPA methodology as:

\[ GDP \equiv p_t^T Y_t^T + p_t^N Y_t^N \\
= w_t^T \theta_t L_t + w_t^N (1 - \theta_t) L_t + r_t K_t \\
= Y_t + p_t^T NX_t^T \]

4 Accounting for the Mexican Appreciation

This section describes the main exercise in our paper. We compute the transitional path for the small open economy described in the previous section, starting from an initial stationary equilibrium and given exogenous sequences for sectoral TFP \( A_t^T, A_t^N \), for international interest rates \( r_t^* \) and total employment \( \overline{L}_t \) taken from the data. We then analyze the resulting sequences for the domestic relative price of tradables in order to assess the ability of the model to generate an appreciation of the RER as the one observed in Mexico. We also compare model predictions to data on labor reallocation across sectors.

4.1 Calibrating the Model

The model is calibrated to Mexican data. A few parameters have a direct empirical counterpart, while others are determined simultaneously matching a set of calibration targets. Notice that, although our model is forced to be consistent with some basic observations for the Mexican economy, no data on the real exchange rate nor on the relative price of tradable
<table>
<thead>
<tr>
<th>Statistic</th>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Labor income share in tradable sector</td>
<td>$\alpha_T$</td>
<td>0.48</td>
</tr>
<tr>
<td>Labor income share in non-tradable sector</td>
<td>$\alpha_N$</td>
<td>0.35</td>
</tr>
<tr>
<td>Elasticity of substitution T and N goods</td>
<td>$\rho$</td>
<td>-1.0</td>
</tr>
<tr>
<td>Ratio of tradable to non-tradable goods in domestic demand</td>
<td>$\gamma$</td>
<td>0.23</td>
</tr>
<tr>
<td>Long run world interest rate</td>
<td>$\beta$</td>
<td>0.957</td>
</tr>
<tr>
<td>Intertemporal elasticity of substitution</td>
<td>$\sigma$</td>
<td>2.0</td>
</tr>
<tr>
<td>Depreciation rate</td>
<td>$\delta$</td>
<td>0.05</td>
</tr>
<tr>
<td>Stationary fraction of labor in tradable sector</td>
<td>$A^T_0/A^N_0$</td>
<td>0.516</td>
</tr>
<tr>
<td>Stationary fraction of net exports in GDP</td>
<td>$B_0$</td>
<td>-0.045</td>
</tr>
<tr>
<td>Minimum distance between data and model</td>
<td>$\psi$</td>
<td>32.25</td>
</tr>
<tr>
<td>- Total real GDP per worker</td>
<td>$\phi$</td>
<td>145.64</td>
</tr>
<tr>
<td>- Relative wage between T and N sectors</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 3: Calibration of the Model

goods is used to calibrate the parameters.

We use the 1980 Mexican input-output matrix to calibrate income shares in the production functions. Unfortunately, such matrices are not computed regularly. We measure payments to labor relative to GDP at factor prices for each sector and we adjust the labor income share by taking into account the income of the self-employed, following Gollin (2002) and Garcia-Verdú (2005). Since self-employment income is not available by sector, we compute an aggregate adjusted labor income share and scale sectoral shares by the same factor. We obtain a capital income share in the tradable sector of 0.48, and 0.35 in the non-tradable sector. As expected, the tradable sector is capital intensive.

For the final good aggregator, we choose the value of $\rho$ in order to have an elasticity of substitution of $\frac{1}{2}$ between tradable and non-tradable goods, similar to Stockman and Tesar (1995). We then calibrate the weight of tradable goods in the production of final goods, $\gamma$, using information on final domestic demand for tradable and non-tradable sectors in Mexico from the 1980 input-output matrix. Given the value of $\rho$, we use the first order conditions of the final goods producer, yielding the relative price of tradable goods as a function of the ratio of $Q^T$ to $Q^N$. Choosing units as to normalize the 1980 relative price of tradables over non-tradables goods to one, the implied weight of tradable goods is $\gamma = 0.23$.

On the consumption side, we choose a standard risk aversion coefficient of 2 implying an intertemporal elasticity of substitution of $\frac{1}{2}$. The exogenous sequence of international
interest rates \( \{r^*_t\} \) was computed as the real interest rate in the US plus a Mexican specific spread (or country risk) as in Meza and Quintin (2007). Since the first observation available is from the end of 1990, we extrapolate the 1988-1989 values using information on domestic Mexican interest rates in dollars. Figure 7 shows the resulting sequence. Notice the long run fall in the international interest rate for Mexico, associated to a process of financial liberalization, with a short run jump around the 1995 crisis. For the purpose of the exercise, from 2003 onwards we assume a constant long run rate of 4.5%, that we use to calibrate the discount factor \( \beta \). The depreciation rate \( \delta \) is 5%.

Given these parameters, we jointly calibrate the initial relative TFP between the two sectors \( A^T_0/A^N_0 \) and the initial stock of wealth of the economy \( (B_0) \) so as to obtain in the initial stationary equilibrium of the model: (i) a fraction of labor allocated to the tradable sector of 40%, and (ii) a fraction of net exports in GDP of 2.3%. These two numbers are consistent with Mexican data for 1988. The remaining sequences for \( \{A^T_t, A^N_t\} \) are constructed given the initial ratio \( A^T_0/A^N_0 \) and using the rates of growth of TFP for each sector computed from the data (see Figure 5 again). From 2003 onwards we assume constant TFP factors equal to their 2002 level.

This leaves us with two parameters (\( \psi \) and \( \phi \)), associated to the adjustment costs for capital and labor. Since the adjustment cost for capital controls the speed of capital accumulation, GDP growth seems a natural target for the calibration. Similarly, the adjustment cost for labor can be pinned down by deviations from wage equalization across sectors, which are entirely due to labor market frictions in our model. Therefore, we jointly choose the values of these two parameters in order to minimize the distance between the time series generated by the model along the equilibrium transition path described in the next section and the Mexican 1998-02 data for: (i) the real total GDP per worker, and (ii) the relative wage between tradable and non-tradable sectors. A summary of the calibration is presented in Table 3.

### 4.2 Equilibrium Path and the Relative Price of Tradable Goods

We compute the transitional equilibrium path of the model as follows. First, we obtain the initial conditions for capital \( (K_0) \), bonds \( (B_0) \), and labor allocation \( (\theta_{-1}) \) from the stationary
equilibrium of the model given the initial (1988) values for $A^T_0$, $A^N_0$, $r^*_0$, and $L_0$. In particular, we compute this initial steady state assuming a world interest rate $r^*_0 = 20\%$ and adjusting the discount factor accordingly. All other parameters are the same as in Table 3.

Starting from this stationary equilibrium, we then feed the model with the exogenous sequences for sectoral TFP $\{A^T_t, A^N_t\}$, international interest rates $\{r^*_t\}$ and total employment $\{L_t\}$ constructed from the data. We assume that in $n = 100$ periods (years) the economy reaches the new steady state, given the final values for $A^T_n$, $A^N_n$, $r^*_n$, and $L_n$. These values are assumed to be equal to their 2002 counterpart in the data, i.e., from 2003 onwards we assume they remain constant. Solving the system of first order conditions for each of the $n$ periods we obtain the equilibrium transition path for the endogenous variables of the model.3

Figure 9 reports the time series obtained from the first fifteen observations generated by our model and compares them to the actual 1988-02 Mexican data. By construction, the model reproduces very well the trends for GDP per worker and relative wages across sectors, as the adjustments costs for capital and labor were calibrated to that effect. A better measure of the success of the model is how well it captures the structural shift of labor from the tradable to the non-tradable sector, as well as the downward trend in relative output per worker of the non-tradable sector. The model does this successfully. Moreover, as seen in panel (e) of Figure 9, the model generates a large decline in the domestic relative price of tradable goods, defined as $p^T_t$ in the model. Looking only at endpoints, the model accounts for 60% of the change in this relative price which, as discussed in Section 2, is responsible for most of the RER appreciation in Mexico.4

To summarize, our model generates a large fraction of the decline in the domestic relative price of tradable goods observed in the data and a structural change in the allocation of labor with two main ingredients: (i) the differential TFP growth between tradable and

---

3The design of our experiment is subject to some obvious criticisms: Was the Mexican economy before 1988 in a steady state? Do agents perceive a stationary environment after 2002? Probably not. Nevertheless, our procedure ties our hands in terms of choosing initial and final conditions for the model. In this sense, among other equally arbitrary choices, we believe ours provides the most discipline to the experiment.

4The model has some trouble matching the data around the 1995 Mexican crisis. This is so for at least two reasons. First, we are assuming that the 1995 interest rate and productivity shocks were perfectly anticipated, so agents start reacting to it in previous periods. Second, the crisis was the result of a sudden stop of loans from abroad, which we are not considering. As explained before, our focus in this paper is the long run trend of the RER, not the short run depreciation of 1995.
non-tradable sectors, i.e., the Balassa-Samuelson effect, and (ii) a decline in the real interest rate faced by Mexico in the international markets. In the next section we discuss in more detail each channel and provide an assessment of their relative importance.

5 Sources of the Mexican Appreciation

This section accomplishes three things. First, we decompose the decline in the domestic relative price of tradable goods generated by the model in its two main channels, sectoral TFP shocks and the decline in the international interest rate for Mexico. Second, we analyze the role of the adjustment cost of labor for our results. Finally, we analyze the effect of three demand shocks: migration remittances, government expenditures and international reserves accumulation, which have received some attention as potential determinants of the real exchange rate in Mexico.

5.1 Sectoral TFP Shocks vs. Interest Rate Shocks

Our model economy faces two types of shocks: (i) a supply shock, the differential TFP growth in tradable and non-tradable sectors, and (ii) a demand shock, driven by the change in the international interest rate for Mexico.

Let us start with the sectoral TFP shocks. As discussed in Section 2, TFP growth has been unequal across sectors. Between 1988 and 2002, TFP grew at a 1.8% yearly rate in the tradable sector, while TFP in the non-tradable sector remained stagnant (in fact, it declined by 0.4%). In our model, technological progress in the tradable sector reduces the cost of production in this sector, making tradable goods cheaper and appreciating the RER. This is the well known Balassa-Samuelson effect.

The impact of differential productivity growth across sectors on labor reallocation is more ambiguous. The direct effect of TFP changes is to switch resources, including workers, towards the most productive sector. In this case, this is the tradable sector. But there is a second, income effect. As productivity growth makes the economy richer, agents demand more of the two goods. The tradable good can be imported, but the non-tradable good has to be domestically produced so resources move towards this sector. Depending on
Table 4: Accounting for the Mexican Appreciation

<table>
<thead>
<tr>
<th>Change (%) 88-02</th>
<th>Price of Tradables</th>
<th>Relative Labor T/N</th>
</tr>
</thead>
<tbody>
<tr>
<td>Data</td>
<td>-32.1%</td>
<td>-28.9%</td>
</tr>
<tr>
<td>Benchmark Economy</td>
<td>-19.1%</td>
<td>-24.9%</td>
</tr>
<tr>
<td>- No Productivity Shocks</td>
<td>-12.5%</td>
<td>-16.5%</td>
</tr>
<tr>
<td>- No Adjustment Costs for Labor</td>
<td>-16.2%</td>
<td>-38.3%</td>
</tr>
<tr>
<td>- Adding Remittances</td>
<td>-19.1%</td>
<td>-25.2%</td>
</tr>
<tr>
<td>- Adding Changes in Reserves</td>
<td>-18.6%</td>
<td>-26.2%</td>
</tr>
<tr>
<td>- Adding Government Spending</td>
<td>-18.2%</td>
<td>-22.3%</td>
</tr>
</tbody>
</table>

how substitutable tradable and non-tradable goods are in consumption, either effect could dominate.

Figure 10 shows the time series generated by the model shutting down this channel, this is, without sectoral TFP shocks. In this exercise, we still obtain a decline in the relative price of tradable goods, but of only 13% instead of 19% in the benchmark model (see Table 4). Moreover, in this version of the model there is also less labor reallocation to the non-tradable sector compared to what is obtained in the benchmark model and observed in the data, highlighting the importance of the income effect of productivity shocks. We conclude that, roughly speaking, sectoral TFP shocks are responsible for about 1/3 of the Mexican appreciation and structural transformation.

The remaining 2/3 is then accounted for the decline in the interest rate faced by Mexico in international credit markets. In the context of the model, a reduction in the world interest rate provides incentives for agents to borrow more abroad, increasing the current account deficit. Hence, tradable goods become less valuable, their relative price falls and resources shift away towards the non-tradable sector. This is a purely demand effect, which is consistent with the RER appreciation and the structural change in the Mexican economy. It proves to be quantitatively very important.

5.2 The Role of Adjustment Costs for Labor

To analyze the importance of adjustment costs to labor mobility for our results, we ran a version of the model in which these costs are turned off ($\phi = 0$). The results are reported in Figure 11 and Table 4. Without adjustment costs for labor, the model explains about half
of the observed decline in the relative price of tradable goods, less than in the benchmark experiment. Moreover, the model greatly overpredicts the size of labor reallocation towards the non-tradable sector.

Both issues are related. Facing the exogenous sequences of productivity and interest rates, agents want to switch resources from the tradable sector to the non-tradable sector. With adjustment costs, this is done at a slower rate, keeping over time an inefficiently high fraction of labor in the tradable sector and bidding down the wage rate in that sector. Producing tradable goods becomes cheaper, and this is reflected in a decline of its relative price with respect to non-tradable goods, amplifying the RER appreciation.

Adjustment costs for labor are indeed important in our story. Choosing the size of adjustment costs that better matches the evolution of relative wages in the data, as we did in our calibration procedure, provides the required discipline to the exercise. Moreover, although $\phi \approx 145$ seems to be a large number, the amount of resources wasted by reallocating labor represent only between 0.5% and 0.7% of GDP in the model.

5.3 Other Demand Shocks

We finish this section by quantifying the role of other demand shocks in explaining the decline in the relative price of tradables. These shocks are: (i) migration remittances; (ii) foreign reserves accumulation; and (iii) government spending. Although in theory the three shocks have potentially an effect on the size of the Mexican appreciation, we show that their quantitative impact is minor.

5.3.1 Migration Remittances

The importance of immigration for Mexico is difficult to understate. It is estimated that about 9% of the Mexican labor force lives in the US. Not surprisingly, migration remittances constitute a significant flow of income for many families. Its size has been estimated to lie between 1% to 2% of Mexican GDP. According to one measure, reported in Figure 8, migration remittances have also increased over time between 1988 and 2002, from an average of 1% of GDP in the late eighties to about 1.5% of GDP in the late nineties.
The impact of migration remittances on the macroeconomy has been widely debated. In particular, the increase in remittances is one of the usual suspects for the RER appreciation in developing countries (see, for example, Amuedo-Dorantes and Pozo (2004) and recent papers by Durdu and Sayan (2008) and Acosta, Lartey, and Mandelman (2007)). In the context of our model, a transfer from abroad finances an increase in the trade deficit, reducing the relative value of tradable goods. How big is that effect?

To answer this question, we feed our model with an additional shock, migration remittances, modeled as an exogenous transfer of tradable goods from abroad of size determined by the data in Figure 8. The results are hard to distinguish from the benchmark economy. Results are shown in Table 4. Changes in remittances of the size observed in the data have no significant impact on the domestic relative price of tradable goods.

5.3.2 Foreign Reserves Accumulation

We also explore the role of international reserves accumulation in the Mexican appreciation. Figure 8 shows that changes in reserves are on average of the same magnitude as migration remittances, although much more volatile. After the 1995 crisis, the Mexican Central Bank accumulated a large stock of foreign reserves as an insurance against sudden stops. As in other countries following similar policies (see Rodrik (2006) for a discussion), reserves accumulation could potentially achieve two related objectives: (i) to reduce the cost of external financing, and (ii) to mitigate the appreciation of the RER caused by the improved access to credit. Both are relevant for our analysis.

We add international reserves as a non-interest bearing asset whose accumulation is exogenous. An increase in international reserves acts in the opposite direction as a transfer from abroad, reducing the current account deficit and making tradable goods more valuable. Again, the question is whether this mechanism is quantitatively important for the appreciation in Mexico. Not surprisingly, given our previous result for remittances, it is not. Results are shown in Table 4. Feeding the model with the exogenous sequence of changes in reserves from Figure 8 does not change significantly any of the time series generated by the model. It does decrease the fall in the relative price of tradable goods, but by less than one percentage point.
In other words, according to our quantitative model, had the Central Bank not accumulated reserves, the RER in Mexico would have appreciated by a barely noticeable 0.5% more.\(^5\) This seems small compared to other policy alternatives. Consider for example the effect of policies increasing the flexibility of the labor market. According to the previous subsection, eliminating the adjustment cost for labor would have reduced by 2.5 percent points the RER appreciation.

### 5.3.3 Government Expenditures

Government consumption of non-tradable goods is an important component of total government consumption in Mexico. Using the 1980 input-output table, we find that 94% of government consumption is in non-tradable goods. Time series data for 1988-2002 shows that on average 78% of total government consumption is allocated to wages of public employees. Changes in the size of government spending can therefore affect the relative demand for non-tradable goods and their relative price. This mechanism has been empirically studied in De Gregorio and Wolf (1994), Balvers and Bergstrand (2002) and recently by Ricci, Milesi-Ferretti and Lee (2008), which find it to be significant in a panel of countries.

As observed in Figure 8, between 1988 and 2002 government consumption as a fraction of Mexican GDP fell steadily from 12% to 9.8%. Although this is not a large drop, it implies a decrease in the demand for non-tradables, which in theory could increase the relative price of tradable over non-tradable goods and partially offset the RER appreciation. In our model it does, but not by much. Results are shown in Table 4. Assuming that all government consumption is in non-tradables and adding the sequence of observed government expenditure shocks, the model generates a smaller decline in the domestic relative price of tradables. Still, the difference is again less than one percentage point.

\(^5\)This ignores the indirect impact that foreign reserves accumulation might have on the interest rate faced by Mexico in international credit markets, which is exogenous in our setup. Since the external cost of financing was indeed declining during this period, adding this channel could potentially increase the role of foreign reserves accumulation in explaining the Mexican appreciation. But in order to quantify this indirect channel we would need to endogenize the Mexican risk premium, which is outside the scope of the paper.
6 Terms of Trade, Tariffs and the Mexican Appreciation

In this final section, we modify the basic model by adding international differentiation in tradable goods. This version of the model features an importable good which is an imperfect substitute of the domestically produced tradable good. The relative price between the two defines the terms of trade for this economy which, keeping the assumption of a small open economy, are exogenous. This setup allows us to check the robustness of our previous results with respect to deviations from the price of Mexican tradable goods with respect to the foreign price level (the residual discussed in Section 2), generated by terms of trade shocks.

6.1 A Model with International Differentiation of Goods

The basic structure of the model is similar to the one described in Section 3. The main difference is that the final good is now produced aggregating non-tradables and a composite tradable good, itself the result of aggregating domestically produced tradable goods and imports ($M_t$)

$$Y_t = \gamma \left( \left[ \mu \left( Q^T_t \right)^\zeta + (1 - \mu) M_t^\chi \right]^{\frac{1}{\zeta}} \right)^\rho + (1 - \gamma) \left( Q^N_t \right)^\rho^{\frac{1}{\chi}}$$

with the (Armington) elasticity of substitution $1/(1 - \zeta)$. The assumption is that, because of product differentiation, domestically produced tradable goods and imports are not perfect substitutes.

The producer of the final good solves now each period the static problem:

$$\max_{Y_t, Q^T_t, Q^N_t} \left\{ Y_t - p^T_t \left[ Q^T_t - (1 + \tau_t) \frac{M_t}{(p^T_t/p^M_t)^*} \right] - p^N_t Q^N_t \right\}$$

s.t. $$Y_t = \gamma \left( \left[ \mu \left( Q^T_t \right)^\zeta + (1 - \mu) M_t^\chi \right]^{\frac{1}{\zeta}} \right)^\rho + (1 - \gamma) \left( Q^N_t \right)^\rho^{\frac{1}{\chi}}$$

where $(p^T_t/p^M_t)^*$ are the exogenously given terms of trade for this economy and $\tau_t$ represents an import tariff, rebated to the representative consumer as a lump sum transfer.
In equilibrium, markets clear for each domestically produced good,

\[ Q_T^T + X_T^T = Y_T^T \quad Q_N^N = Y_N^N \]

where \( X_T^T \) represents exports of the tradable good. Tariff collection is rebated to the consumer as lump sum transfer \( T_t \):

\[ T_t = \frac{M_t}{(p_T^T/p_M^M)^\ast} \]

Finally, the current account can be constructed as the value of net exports plus interest payments or as the change in the foreign asset position:

\[ CA_t \equiv \left( X_T^T - \frac{M_t}{(p_T^T/p_M^M)^\ast} \right) + r_t^* B_t = B_{t+1} - B_t \]

We will focus on the predictions of the model regarding the domestic relative price of tradables \( p_T^T \). Additionally, this version of the model allows us to construct a real exchange rate which includes the residual exogenously explained by terms of trade shocks, as

\[ RER_t = \frac{p_T^T}{(p_T^T/p_M^M)^\ast} \]

### 6.2 Revisiting our Quantitative Results

To compute the new version of the model we need first to calibrate two new parameters in the Armington aggregator, \( \zeta \) and \( \mu \), and recalibrate the parameters \( \gamma, A_T^0/A_N^0, B_0, \psi \) and \( \phi \) to be consistent with the same calibration targets. We set initial terms of trade \( (p_0^T/p_0^M)^\ast = 1 \), and set the initial import tariff \( \tau_0 \) to 10%, the value used in Kehoe and Ruhl (2009) for 1988. We set \( \zeta = 0.5 \) to have an elasticity of substitution of 2 between imports and tradable goods, as in Kehoe and Ruhl (2009), and calibrate \( \mu \) and \( \gamma \) using the 1980 input-output table. Finally, we follow the same strategy as with the basic model in order to calibrate \( A_T^0/A_N^0 \) and \( B_0 \) to match the initial labor allocation and net exports, and \( \psi \) and \( \phi \) to minimize the distance between the model’s real GDP and relative wage and the corresponding series in the data. All the remaining parameters have the same values reported in Table 3.
Statistic | Parameter
--- | ---
Elasticity of substitution between tradable goods and imports | 2 | $\zeta$
Ratio of imports to tradable goods | 0.56 | $\mu$
Ratio of tradable to non-tradable goods in domestic demand | 0.55 | $\gamma$
Stationary fraction of labor in tradable sector | 40% | $A^T_0 / A^N_0$
Stationary fraction of net exports in GDP | 2.3% | $B_0$
Minimum distance between data and model
- Total real GDP per worker | | $\psi$
- Relative wage between T and N sectors | | $\phi$

Table 5: Calibration of the Model with Terms of Trade Shocks

6.2.1 The Role of Terms of Trade

As before, we compute the transitional equilibrium path of the new model as follows. First, we obtain the initial conditions for capital, bonds, and labor allocation from the stationary equilibrium of the model. Then, we feed the model with the exogenous sequences for sectoral TFP, international interest rates, total employment and terms of trade \( \left\{ \left( \frac{p^T_t}{p^M_t} \right)^* \right\} \) observed in the data. The sequence for the terms of trade corresponds to the (inverse of the) one reported in Figure 3, while for now we keep tariffs constant during the whole period.

Figure 12 reports the time series obtained from the first fifteen observations generated by our model and compares them to the actual 1988-02 Mexican data. The results are similar to the ones reported in Figure 9. Once recalibrated to match the trends for real GDP per worker and relative wages across sectors, the model with terms of trade shocks also captures the structural shift of labor from the tradable to the non-tradable sector and the change in the composition of output. As reported in Table 6, looking only at endpoints the model with terms of trade shocks accounts for 54% of the change in the domestic relative price of tradables, compared to 60% in the benchmark model. The model also accounts for 69% of the RER appreciation, although it should be noticed that this number includes the contribution of exogenous terms of trade.

Previous studies (see, for example, De Gregorio and Wolf (1994) and Cashin, Cespedes and Sahay (2004)) have found and important role for terms of trade as determinants of real exchange rate movements, especially in commodity exporters countries. Our results are consistent with these findings. The small improvement in terms of trade observed in Mexico
between 1988 and 2002 in fact had a direct impact in the RER appreciation by increasing the price of Mexican tradable goods with respect to the foreign price level. However, the improvement in terms of trade slightly reduces the decline in the domestic relative price of tradable goods generated by our model.\footnote{See Edwards and Van Wijnbergen (1987) for a detailed discussion on the theoretical effects of changes in terms of trade and tariffs on relative prices and on the RER, in particular on the income and substitution effects involved.}

### 6.2.2 The Role of Import Tariffs Reduction

In our last experiment we analyze the role of the import tariffs reduction following the free trade agreements negotiated by Mexico at the beginning of the 1990’s, in particular NAFTA. Following Kehoe and Ruhl (2009), we model the tariff reduction in a simplified way: starting from a 10% import tariff in 1988, we assume a reduction to 5% in 1994, followed by a 0.5 percentage point per year decline from 1994 onwards. We compute again the equilibrium path for the model adding this new exogenous shock, and report the main results in Table 6. As observed, the effects of this tariff cut on the labor allocation across sectors and the domestic relative price of tradables are negligible, probably because import tariffs were already low at the beginning of the period studied.

To summarize this section’s findings, the results obtained with the benchmark model in Section 4 are robust to deviations from the price of Mexican tradable goods with respect to the foreign price level, generated by exogenous terms of trade shocks, and to NAFTA’s tariff reductions. None of these two shocks on their own played an important role in explaining the decline in the domestic relative price of tradable goods.

<table>
<thead>
<tr>
<th>Change (%) 88-02</th>
<th>Price of Tradables</th>
<th>Relative Labor T/N</th>
</tr>
</thead>
<tbody>
<tr>
<td>Data</td>
<td>-32.1%</td>
<td>-28.9%</td>
</tr>
<tr>
<td>Benchmark Economy</td>
<td>-19.1%</td>
<td>-25.2%</td>
</tr>
<tr>
<td>Model with Terms of Trade Shocks</td>
<td>-17.5%</td>
<td>-25.3%</td>
</tr>
<tr>
<td>- Adding Import Tariffs Reduction</td>
<td>-16.6%</td>
<td>-25.2%</td>
</tr>
</tbody>
</table>

Table 6: Accounting Using the Model with International Goods Differentiation
7 Conclusions

Using a two sector neoclassical growth model of a small open economy, we identify two main sources of the Mexican appreciation: (i) differential TFP growth across tradable and non-tradable sectors, and (ii) a decline in the real interest rate faced by Mexico in the international markets, associated to a process of financial liberalization. These two channels explain approximately 60% of the change in the domestic relative price of tradables. The results are robust to the inclusion of terms of trade into the model. Contrary to conventional wisdom, we find no important role for migration remittances, government spending, foreign reserves accumulation or import tariffs reduction. Additionally, our model is quantitatively consistent with the observed reallocation of labor from tradable to non-tradable sectors.

One important question which remains open is: are the two identified channels exogenous and independent of each other? One could think of a story in which productivity growth causes an endogenous reduction in the country risk premium by reducing the probability of default, as in Mendoza and Yue (2008). Or even if we assume that the country specific interest rate is exogenous, changes in the cost of credit might affect the productivity of firms in a model of financial frictions. Moreover, as shown in Pratap and Urrutia (2008), these changes in the cost of credit affect differently measured TFP in the tradable and non-tradable sectors, providing a potential explanation to differential productivity growth. A quantitative assessment of these transmission mechanisms which uses the Mexican appreciation as a natural experiment is an interesting topic for future research.

References


Figure 1: Evolution of the Real Exchange Rate in Mexico, 1988-2002

Figure 2: Real Exchange Rate and the Domestic Relative Price of Tradable Goods
Figure 3: Terms of Trade and the Residual

Figure 4: Decomposing the Evolution of the Relative Price of Tradable over Non-Tradable Goods
Figure 5: Evolution of Total Factor Productivity in Tradable and Non-Tradable Sectors

Figure 6: Reallocation of Labor and Capital Between Tradable and Non-Tradable Sectors
Figure 7: International Interest Rate for Mexican Debt (Including Country Premium)

Figure 8: Other Demand Shocks for the Mexican Economy
Figure 9: Equilibrium Transition for the Benchmark Economy
Figure 10: Transition without Sectoral Productivity Shocks
Figure 11: Transition without Adjustment Costs for Labor
Figure 12: Equilibrium Transition for the Model with Terms of Trade Shocks